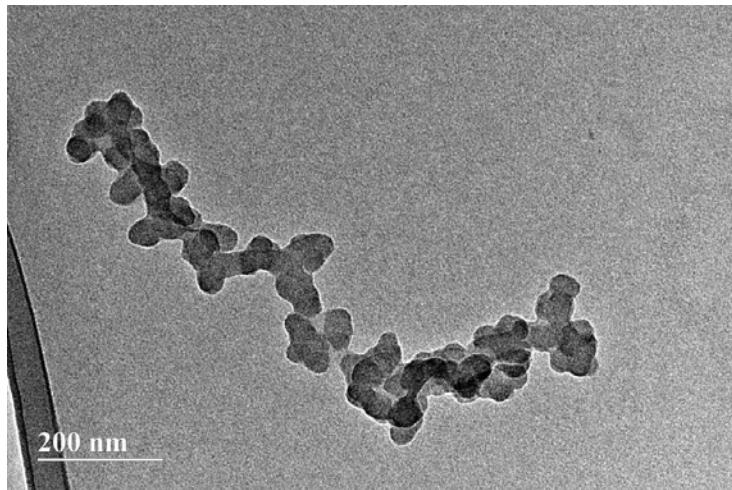




Soot and Radiation



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Acknowledgments:
K. Allan, P. Anderson, J. Castillo, H. Guo,
V. Lecoustre, L. Li, J. Maun, NASA, NIST, NSF



What is soot?

Soot: small solid carbonaceous solids formed in gas-phase flames.

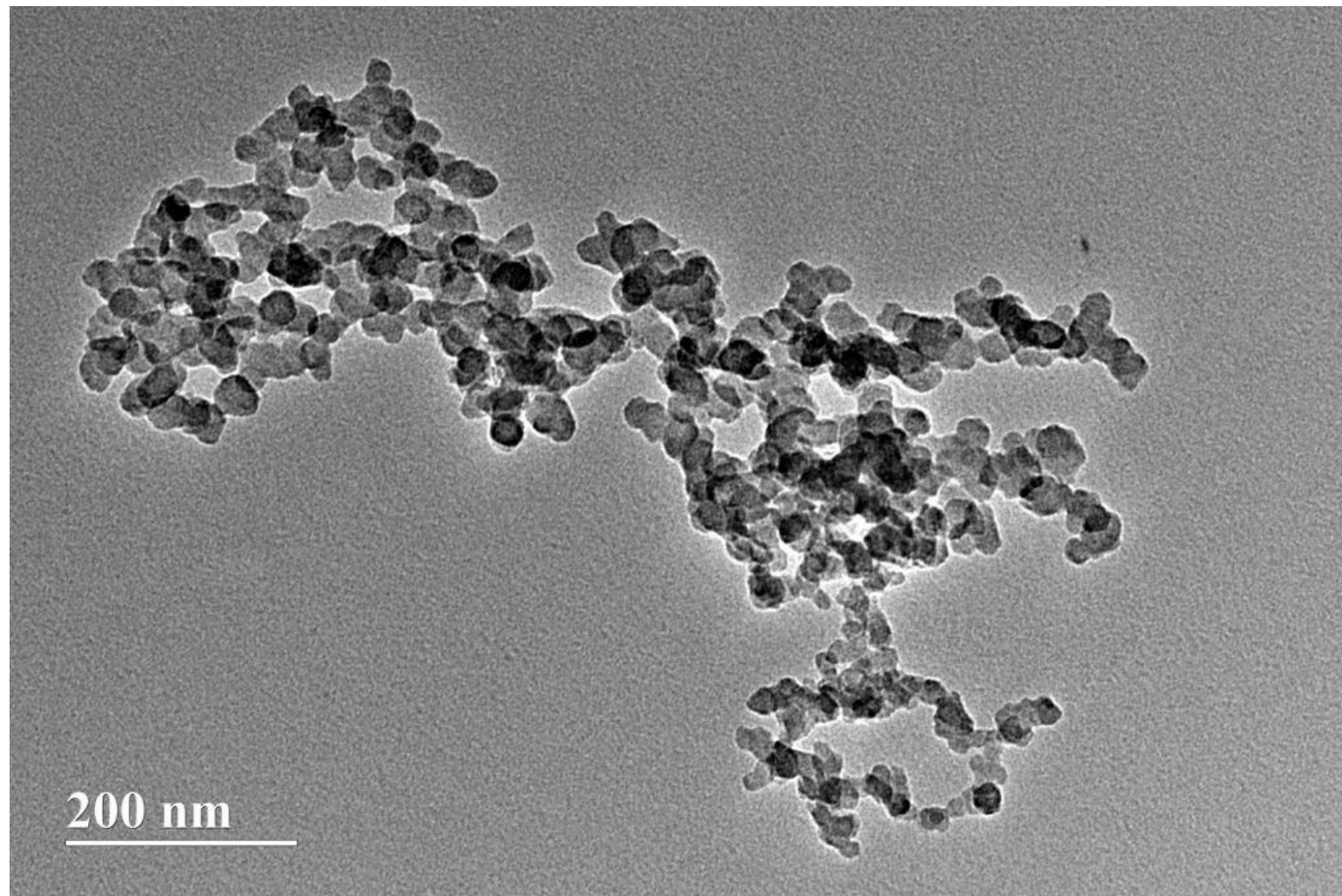
Pyrogenic carbon, aka black carbon: soot, char, and biochar.

Char: solid pyrogenic carbonaceous solids resulting from incomplete combustion.

Biochar: char made from waste biomass for soil amendment and carbon sequestration.



What is soot?



Anderson (2019)

What is smoke?

Smoke: visible materials emitted from a fire.

Most smoke consists of soot (black), oil droplets (blue), water droplets (white), char (black), and ash (white or gray).



Soot and char are black
wikipedia



Oil droplets are blue
wikipedia



Water droplets and ash are white
New York Times

The New York Times

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letters to nature

TINY BITS OF SOOT TIED TO ILLNESSES

E.P.A. Finds the Strongest Link Yet to Support Restrictions

By ANDREW C. REVKIN

In a new review of the science behind its program to purge fumes from the air, the Environmental Protection Agency has concluded that there is a stronger link than ever between the tiniest soot particles and thousands of premature deaths each year.

The analysis, still being revised, considered more than 1,000 new health studies produced since the agency proposed rules in 1987 aimed to cut levels of soot and other smog ingredients produced mostly by power plants and vehicles. The proposed rules are still under review, and the final analysis could be a crucial factor in the Bush administration's decision about how tough the final rules should be.

From the start, business had

The dark side of aerosols

Melina D. Andrea

According to new modelling calculations, black carbon in the atmosphere exerts a large warming influence on global climate. Curbing emissions of this pollutant may be advisable both on climate and on human health grounds.

For a while, it looked as if the greenhouse gases were the Earth and sulfate aerosols could do it down. Sulfate aerosol particles in the atmosphere scatter sunlight back into space, they reduce the amount of energy that the planet absorbs. It's like a sunshade in much the same way as a coat of light paint does a car—only that they are dark paint. But this simplistic view grows the fact that aerosol particles in the air are not white but grey, mostly because they contain soot particles from the incomplete combustion of fuels. And the sootier grey the particles are, the more energy they can absorb, heating the air.

It has been known for quite some time that aerosols may balance the cooling effect of the sulfate component, the largest single contributor to aerosol cooling.



Figure 1: A plume of black carbon. Knowledge of the global sources and distribution of black carbon is poor, and better atmospheric chemistry modelling is needed to evaluate its effect.

news and views

Strong radiative heating due to the mixing state of black carbon in atmospheric aerosols

Mark Z. Jacobson

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Aerosols affect the Earth's temperature and climate by altering the radiative properties of the atmosphere. A large positive component of this radiative forcing from aerosols is due to black carbon—soot—that is released from the burning of fossil fuel and biomass, and, as a sootier smog, makes fires, but the forcing is affected by how black carbon is mixed with other aerosol constituents. From studies of aerosol radiative forcing, it is known that black carbon can exist in one of several possible mixing states: distinct from other aerosol particles (externally mixed) or unaccompanied within dense (internally mixed) or a black-carbon core could be surrounded by a well-mixed shell. But so far it has been assumed that aerosols exist predominantly as an external mixture. Here I simulate the evolution of the chemical composition of aerosols, finding that the mixing state and direct forcing of the black-carbon component approach those of an internal mixture, largely due to coagulation and growth of aerosol particles. This finding implies a higher positive forcing from black carbon than previously thought, suggesting that the warming effect from black carbon may nearly balance the net cooling effect of other anthropogenic aerosol constituents. The magnitude of the direct radiative forcing from black carbon itself exceeds that due to CO_2 , suggesting that black carbon may be the second most important component of global warming after CO_2 , in terms of direct forcing.

Soot in fires



Hickory Record, 2013

- Most fire deaths are associated with smoke inhalation, not burns.
- Soot emission is associated with CO emission.
- In many fires radiation is the dominant mode of heat transfer and is dominated by soot.
- Numerical fire models rely on accurate and simple soot models.



Soot benefits and hazards



Benefits

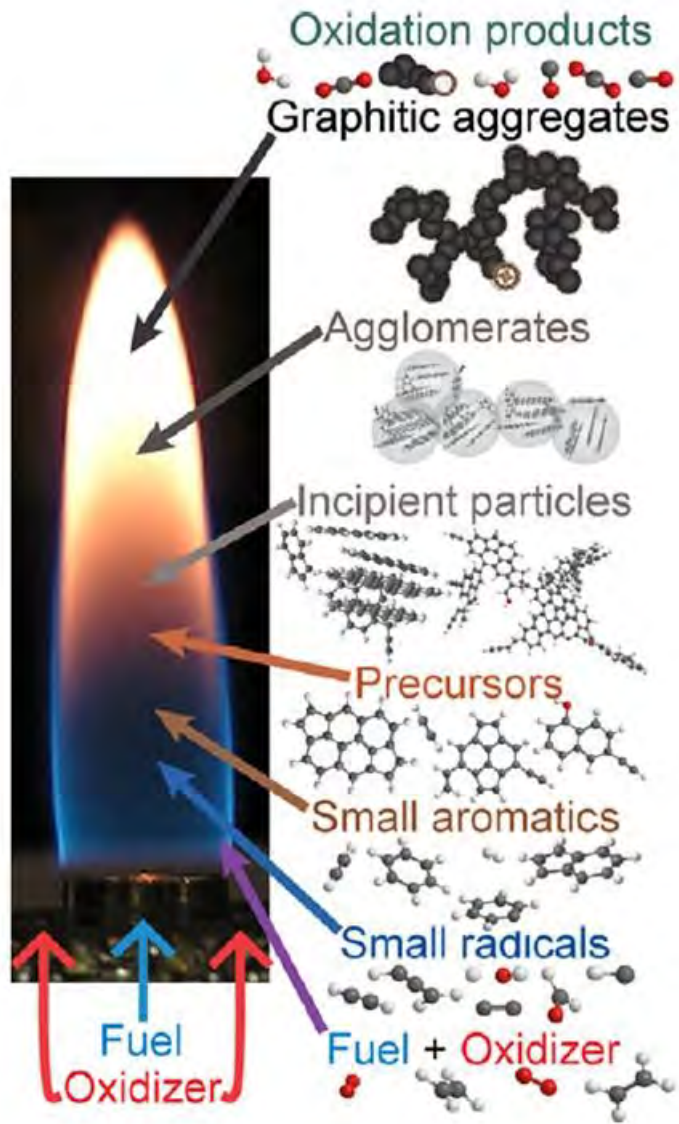
Radiation in boilers
Rubber additive
Printer toner
Pigments
Lubrication
Filtration
Candles

Hazards

60,000 US deaths annually
Cytotoxic, carcinogenic
CO emission
Climate change
Fire spread
Fire obscuration
Property damage
Radiation in engines

“Soot formation is one of the most complex phenomena in combustion, involving complicated interactions between combustion chemistry, fluid mechanics, mass/heat transport, and particle dynamics, so that despite decades of active research, many gaps still remain in our understanding of soot.” (Wang and Chung, PECS 2019).

Soot chemistry



Oxidation

Aggregation

Growth. Agglomeration, coagulation, dehydrogenation, solidification. Primary particles with $d = 10 - 50$ nm, $C/H = 10 - 20$.

Nucleation. Aka nascent particles or nano-organic carbon. Can be disordered (if lean) or stacked (if rich). Liquid-like. $C/H = 1.4 - 2.5$ and $d = 1 - 6$ nm.

Precursor formation, aka PAH

e.g., OH, O, H, CH, CH₂, C₂H₂

e.g., heptane and air



Soot chemistry: nucleation



- Acetylene as a surrogate for soot nucleation is reasonably accurate. There are three widely used models:

$$J_{Moss} = 6 \times 10^6 \bar{\rho}^2 N_A \sqrt{T} \exp\left(\frac{-46100}{T}\right) X_{C_2H_2}$$

$$J_{Leung} = \frac{2}{C_m} N_A 1.7 \exp\left(\frac{-7548}{T}\right) C_{C_2H_2}$$

$$J_{Fairweather} = \frac{2.7 \times 10^6}{\rho_s C_m} N_A \exp\left(\frac{-46100}{RT}\right) C_{C_2H_2}$$

Wang et al. (Energies 2019)

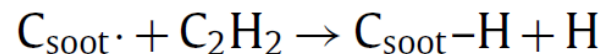
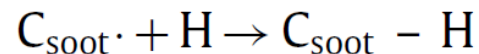
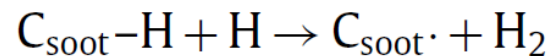


Soot chemistry: growth

- About 90% of the soot mass comes from growth, not nucleation.
- The simplest model is Leung et al. (CST 1991):

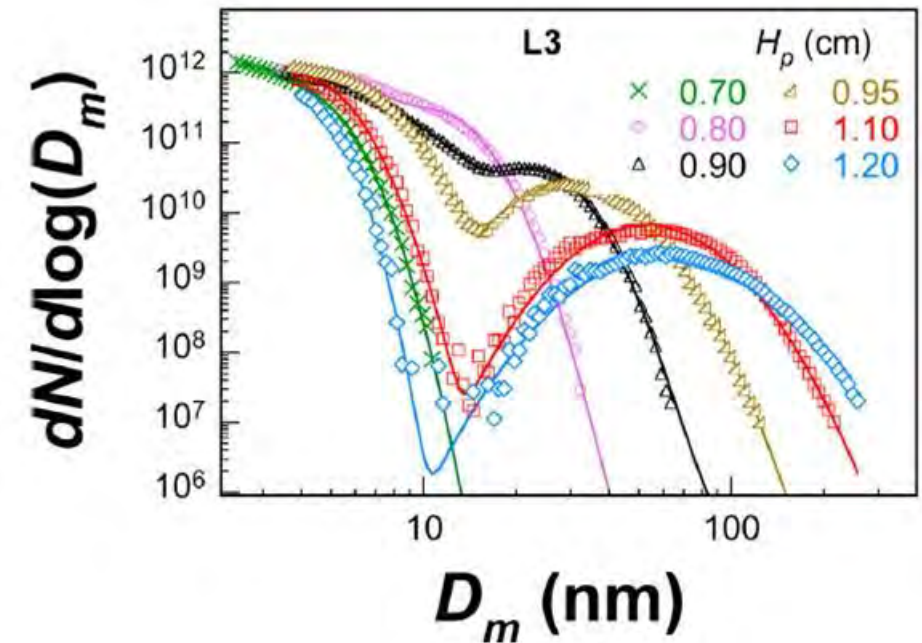
$$\omega_g = k_g(T)[C_2H_2] \sqrt{\pi \left(\frac{6M_c}{\pi \rho_c} \right)^{2/3} [C]^{1/3} (\rho N)^{1/6}}$$

- For improved accuracy the HACA (hydrogen-abstraction carbon addition) is often used. Frenklach and Wang (PCI 1991):



- Whether soot surface growth via PAH is important is a hot topic of debate.

- Soot surface area controls the growth and oxidation rates, and the radiative and thermophoretic behavior.
- Monte-Carlo methods are the most accurate (and costly).
- Sectional methods track the number of soot primary particles in each of ~ 50 size bins.
- The method of moments of the particle size distribution function can accurately reproduce the PSD with 3 – 6 moments.
- Bimodal PSDs are common.



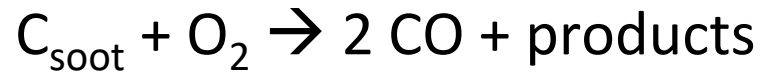
Gu et al. (CNF 2016)



Soot chemistry: oxidation



- Soot is mostly oxidized in flames by OH and O₂, with smaller contributions from O, H₂O, and CO₂:



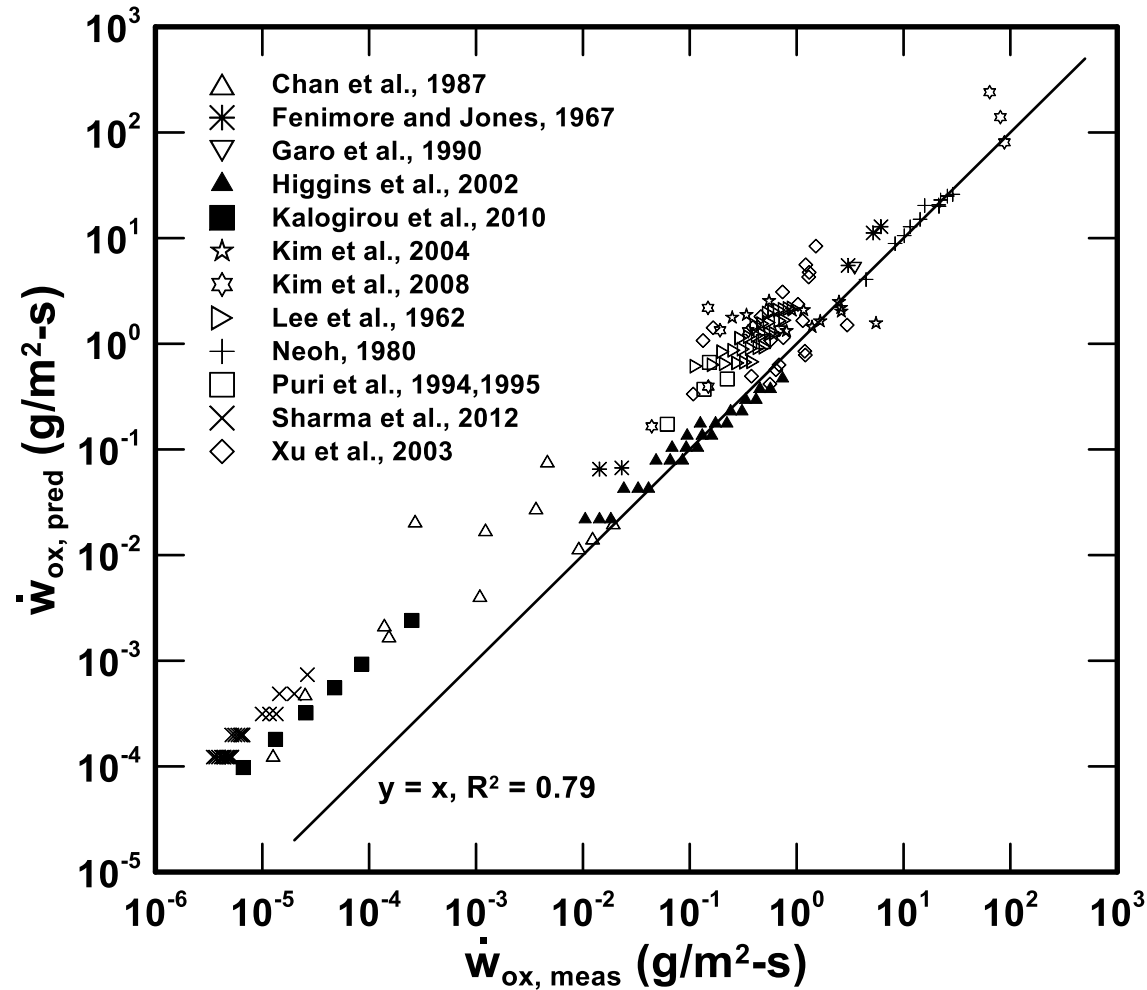
- For OH, Guo et al. (Fuel 2016) recommend:

$$\dot{W}_{\text{ox,OH}} = (1.27 \times 10^{-3} \text{ K}^{0.5} \text{ s/m}) p_{\text{OH}} T^{-0.5}, \text{ i.e., } \eta_{\text{OH}} = 0.10,$$

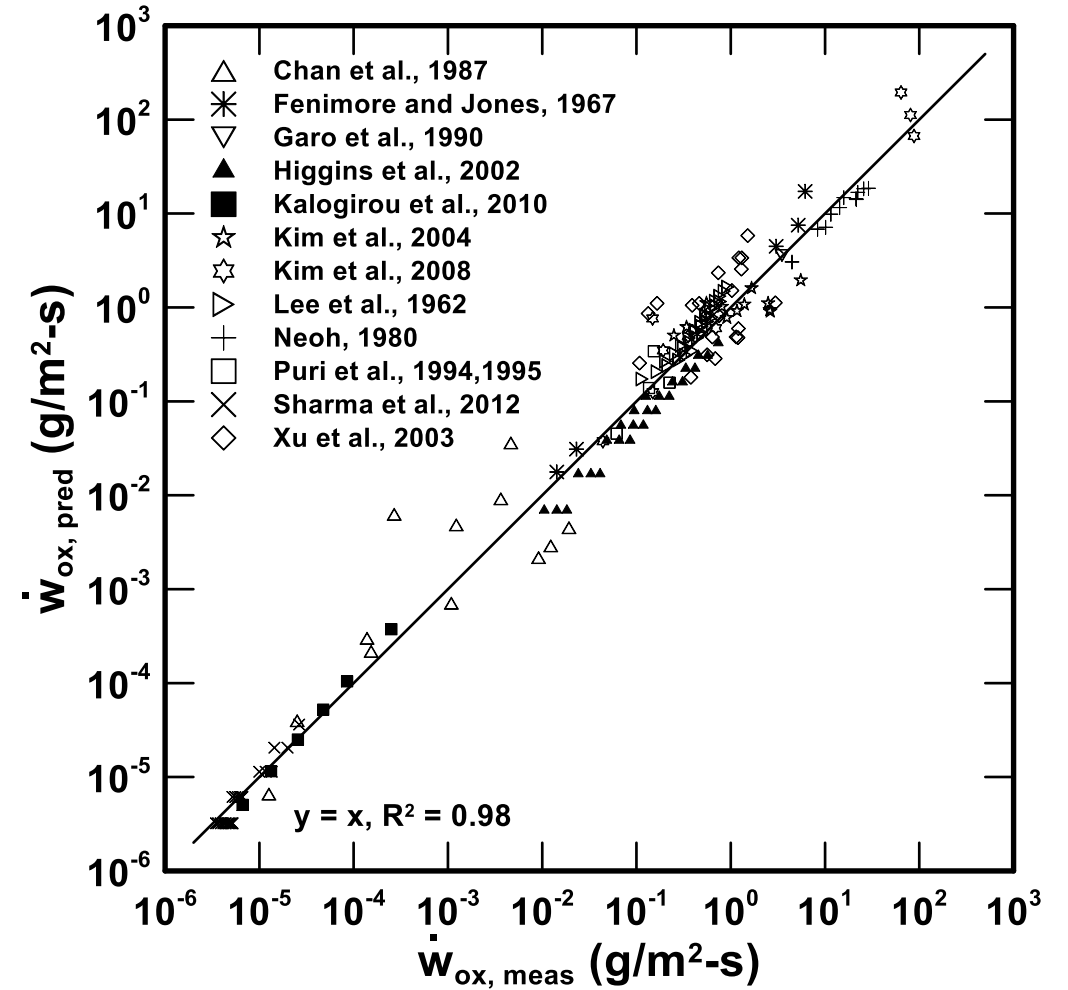
- The most widely used O₂ model is Nagle and Strickland-Constable (1962), but this generally overpredicts the rates. Instead, Guo et al. (Fuel 2016) recommend:

$$\dot{W}_{\text{ox,O}_2} = (15.8 \text{ K}^{0.5} \text{ s/m}) p_{\text{O}_2} T^{-0.5} \exp\left(\frac{-195 \text{ kJ/mol}}{R_u T}\right).$$

Soot oxidation rates

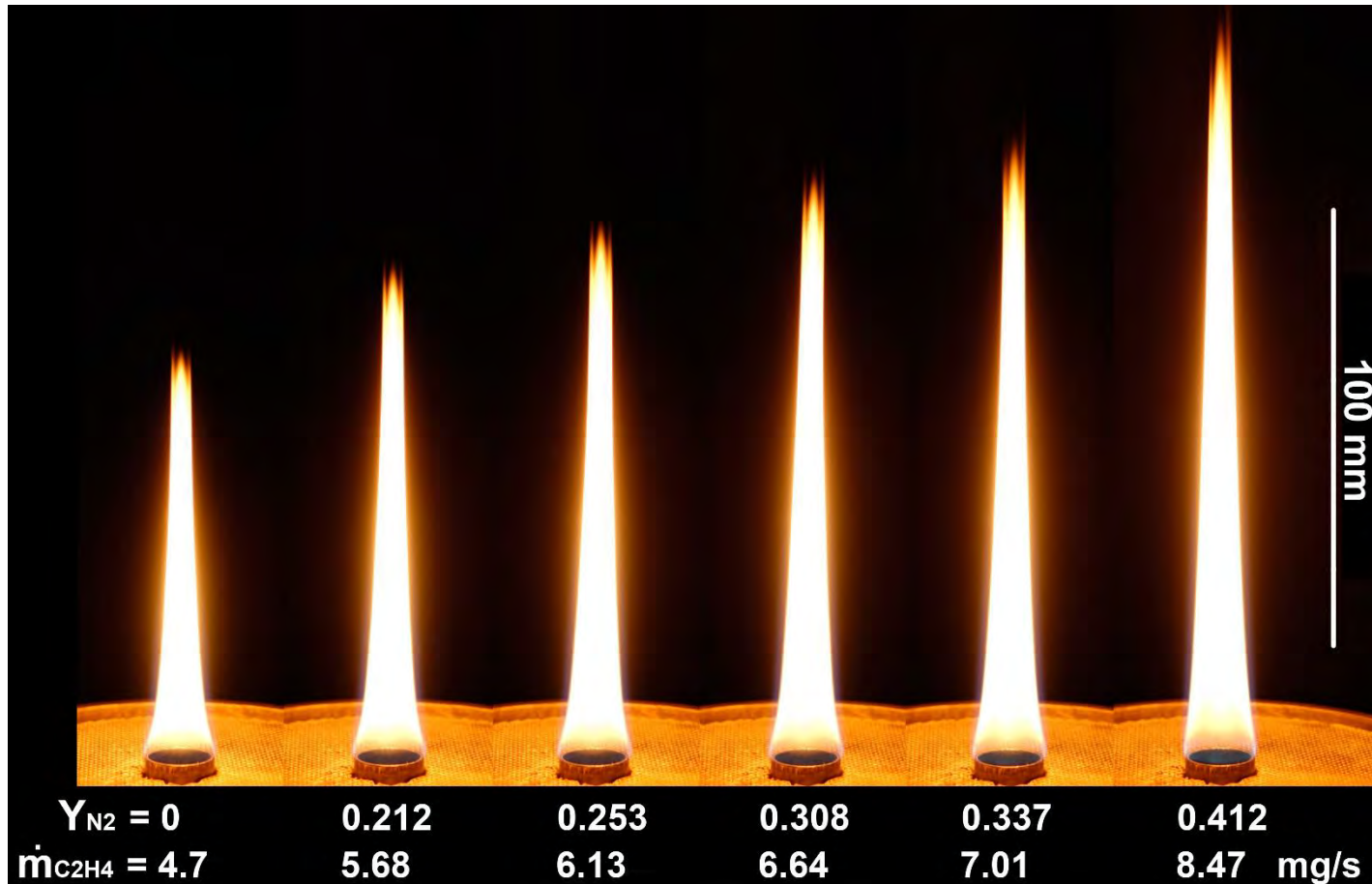


Neoh et al. for OH and NSC for O₂.



Guo et al. (Fuel 2016)

Laminar smoke points



Li and Sunderland (FSJ 2013)

- A laminar smoke point is the condition and length of the incipient sooting of a diffusion flame.
- Smoke points are the prevailing measure of fuel sooting tendency in diffusion flames.
- Numerical fire models use smoke points, e.g., FDS, FireFOAM, Lautenberger et al. (FSJ 2005).



What causes smoke points?



There have been 3 leading explanations of smoke points:

1. Smoke points occur when T falls below 1300 K prior to soot burnout.
2. Smoke points occur when radiative loss fractions exceed 0.2 – 0.3.
3. Smoke points occur when t_{res} is long or when t_{form} / t_{oxid} is high.

Normalized smoke points

Formula	Name	NSP±CI, num	Studies ^a	Formula	Name	NSP±CI, num	Studies
<i>Alkanes</i>				C ₆ H ₁₀	Cyclohexene	38.7±6.3	2-4,7,11
C ₂ H ₆	Ethane	319±153	4,6	C ₆ H ₁₂	1-Hexene	55.2±12.5	2-5,11
C ₃ H ₆	Cyclopropane	25.9	4	C ₇ H ₁₂	4-Methylcyclohexene	23.5	8
C ₃ H ₈	Propane	202±82	4,6	C ₇ H ₁₄	1-Heptene	70.1±15.6	2-4
C ₄ H ₁₀	n-Butane	175±33	4,6	C ₇ H ₁₄	2-Heptene	73.8±11.0	3,4
C ₄ H ₁₀	Isobutane	96.3	4	C ₈ H ₁₂	1,5-Cyclooctadiene	20.0	8
C ₅ H ₁₀	Cyclopentane	58.0±13.5	2-4,11	C ₈ H ₁₄	2,5-Dimethyl-1,5-hexadiene	11.8	4
C ₅ H ₁₂	n-Pentane	163±25	2,4,5,9	C ₈ H ₁₆	1-Octene	56.7±20.9	3,8,10,11
C ₅ H ₁₂	Isopentane	104	2	C ₈ H ₁₆	2-Octene	86.4	3
C ₅ H ₁₂	2,2-Dimethylpropane	59.8	4	C ₉ H ₁₂	1-Nonene	55.2	8
C ₆ H ₁₂	Methylcyclopentane	55.3±1.1	3,4	C ₁₀ H ₁₆	Pinene	18.5	2
C ₆ H ₁₂	Cyclohexane	81.9±16.4	2-4,8,9,11	C ₁₀ H ₂₀	1-Decene	72.4±18.0	2-4,8
C ₆ H ₁₄	n-Hexane	149±24	3,4,9,11	C ₁₁ H ₂₄	1-Dodecene	68.3±30.3	3,8
C ₆ H ₁₄	2-Methylpentane	116±7	3,5	C ₁₁ H ₂₆	1-Tridecene	55.2	8
C ₆ H ₁₄	3-Methylpentane	124±12	3,4	C ₁₄ H ₂₂	1-Tetradecene	67.9±22.6	3,8
C ₆ H ₁₄	2,2-Dimethylbutane	80.1±38.0	2,3	C ₁₅ H ₂₂	1-Hexadecene	69.2±25.1	3,8
C ₆ H ₁₄	2,3-Dimethylbutane	105	3	C ₁₅ H ₂₆	1-Octadecene	82.1	3
C ₇ H ₁₄	Methylcyclohexane	56.6±14.2	2,3,8,11,12	<i>1-Alkynes</i>			
C ₇ H ₁₆	n-Heptane	139±15	2-5,8,9,11	C ₂ H ₂	Ethyne	14.6±8.3	4,6
C ₇ H ₁₆	2-Methylhexane	119	3	C ₃ H ₄	Propyne	10.3	4
C ₇ H ₁₆	3-Methylhexane	120	3	C ₃ H ₄	1-Pentyne	10.8	4
C ₇ H ₁₆	2,3-Dimethylpentane	107	3	C ₆ H ₁₀	1-Hexyne	11.0	4
C ₇ H ₁₆	2,4-Dimethylpentane	102	3	C ₇ H ₁₂	1-Heptyne	18.4±0.8	8,11
C ₈ H ₁₆	cis-1,3-Dimethylcyclohexane	61.1	3	C ₈ H ₁₄	1-Octyne	21.1±0.2	3,8
C ₈ H ₁₆	Ethylcyclohexane	71.3±24.6	3,8	C ₁₀ H ₁₂	1-Decyne	23.5	8
C ₈ H ₁₆	Cyclooctane	56.4	8	C ₁₂ H ₂₂	1-Dodecyne	31.4	3
C ₈ H ₁₈	n-Octane	137±28	3-5,11	<i>Aromatics</i>			
C ₈ H ₁₈	2-Methylheptane	120	3	C ₆ H ₆	Benzene	8.79±1.66	2-4,7,11,12
C ₈ H ₁₈	3-Methylheptane	110	3	C ₇ H ₈	Toluene	8.12±1.60	1,2-5,7,8-11
C ₈ H ₁₈	4-Methylheptane	102	3	C ₈ H ₈	Styrene	5.27±3.49	3,8
C ₈ H ₁₈	3-Ethylhexane	102	3	C ₈ H ₁₀	Xylenes	8.10±1.62	1,2,3,7,8,11
C ₈ H ₁₈	2,2-Dimethylhexane	87.3	3	C ₈ H ₁₀	Ethylbenzene	5.92±1.00	1,3,4,7,8
C ₈ H ₁₈	2,3-Dimethylhexane	107	3	C ₈ H ₂	1-Phenyl-1-propyne	4.70	8
C ₈ H ₁₈	2,2,4-Trimethylpentane	54.3±13.0	2,3,7,8-11,1:	C ₉ H ₂	Indene	5.99±0.23	3,8
C ₈ H ₁₈	2,3,4-Trimethylpentane	59.0	2	C ₉ H ₁₀	α-Methylstyrene	6.09	10
C ₈ H ₁₈	2,2,3-Trimethylpentane	58.1	2	C ₉ H ₁₂	Mesitylene	5.24	3
C ₈ H ₁₈	2-Methyl-3-ethylpentane	89.0	3	C ₉ H ₁₂	Trimethylbenzenes	6.43±1.17	3,8,12
C ₉ H ₂₀	n-Nonane	110±27	4,8	C ₉ H ₁₂	Cumene	6.14±1.78	3,8
C ₉ H ₂₀	Isononane	129	4	C ₉ H ₁₂	n-Propylbenzene	6.86±1.90	3,4,8,12
C ₁₀ H ₂₂	Decalin	25.5±4.3	1,2,3,7,8,12	C ₁₀ H ₈	Naphthalene	3.49	3
C ₁₀ H ₂₂	n-Decane	122±14	3,5,8	C ₁₀ H ₁₀	1,2-Dihydronaphthalene	5.57	12
C ₁₁ H ₂₄	n-Undecane	113±23	3,8	C ₁₀ H ₁₂	Tetralin	7.40±1.21	1,2,3,7,8,10
C ₁₁ H ₂₂	cyclohexylcyclohexane	42.9±8.8	2,3,8	C ₁₀ H ₁₄	p-Cymene	7.90±2.84	2,3,7,8
C ₁₁ H ₂₆	n-Dodecane	107±24	3,8	C ₁₀ H ₁₄	n-Butylbenzene	7.39±2.12	3,8,10
C ₁₁ H ₂₂	n-Tridecane	116	3	C ₁₀ H ₁₄	sec-Butylbenzene	6.97±1.69	3,10
C ₁₄ H ₂₀	n-Tetradecane	120	3	C ₁₀ H ₁₄	tert-Butylbenzene	4.37	3
C ₁₆ H ₂₄	n-Hexadecane	110	2	C ₁₀ H ₁₄	Isobutylbenzene	7.41±2.54	3,10
C ₁₆ H ₂₄	Isohexadecane	33.2	12	C ₁₀ H ₁₄	Diethylbenzenes	6.11	3
<i>Alkenes</i>				C ₁₁ H ₁₀	1-Methylnaphthalene	5.14±0.48	1,3,7,8,12
C ₂ H ₄	Ethene	120±18	4,6,9	C ₁₁ H ₁₀	2-Methylnaphthalene	4.37	3
C ₃ H ₆	Propene	32.8±4.7	4,6,9	C ₁₁ H ₁₆	sec-Pentylbenzene	6.98	3
C ₄ H ₆	1,3-Butadiene	9.23±11.0	4,6	C ₁₁ H ₁₆	tert-Pentylbenzene	6.98	3
C ₄ H ₈	1-Butene	29.1	4	C ₁₁ H ₁₆	n-Pentylbenzene	10.6	8
C ₄ H ₈	2-Butene	30.7	4	C ₁₂ H ₁₂	Dimethylnaphthalenes	4.37	3
C ₄ H ₈	Isobutene	22.6±7.4	4,6	C ₁₂ H ₁₆	Cycloheptylbenzene	7.67±1.06	3,8,10,12
C ₅ H ₈	Cyclopentene	10.3	4	C ₁₂ H ₁₈	Triethylbenzenes	4.37	3
C ₅ H ₈	2-Methyl-1,3-butadiene	15.3	11	C ₁₂ H ₁₈	m-Diisopropylbenzene	10.6	2
C ₅ H ₁₀	1-Pentene	47.1±9.2	2,4,11	C ₁₂ H ₁₂	Benzylbenzene	4.35	10

- Li and Sunderland (CST 2012) correlated the smoke points of 112 hydrocarbons from 12 studies.



Soot diagnostics



- Particle sizes via transmission electron microscopy (TEM), light scattering, or mass spectrometry.
- Soot temperatures via pyrometry.
- Soot concentrations via laser extinction, soot optical emissions, or laser-induced incandescence (LII).



Soot as temperature sensor



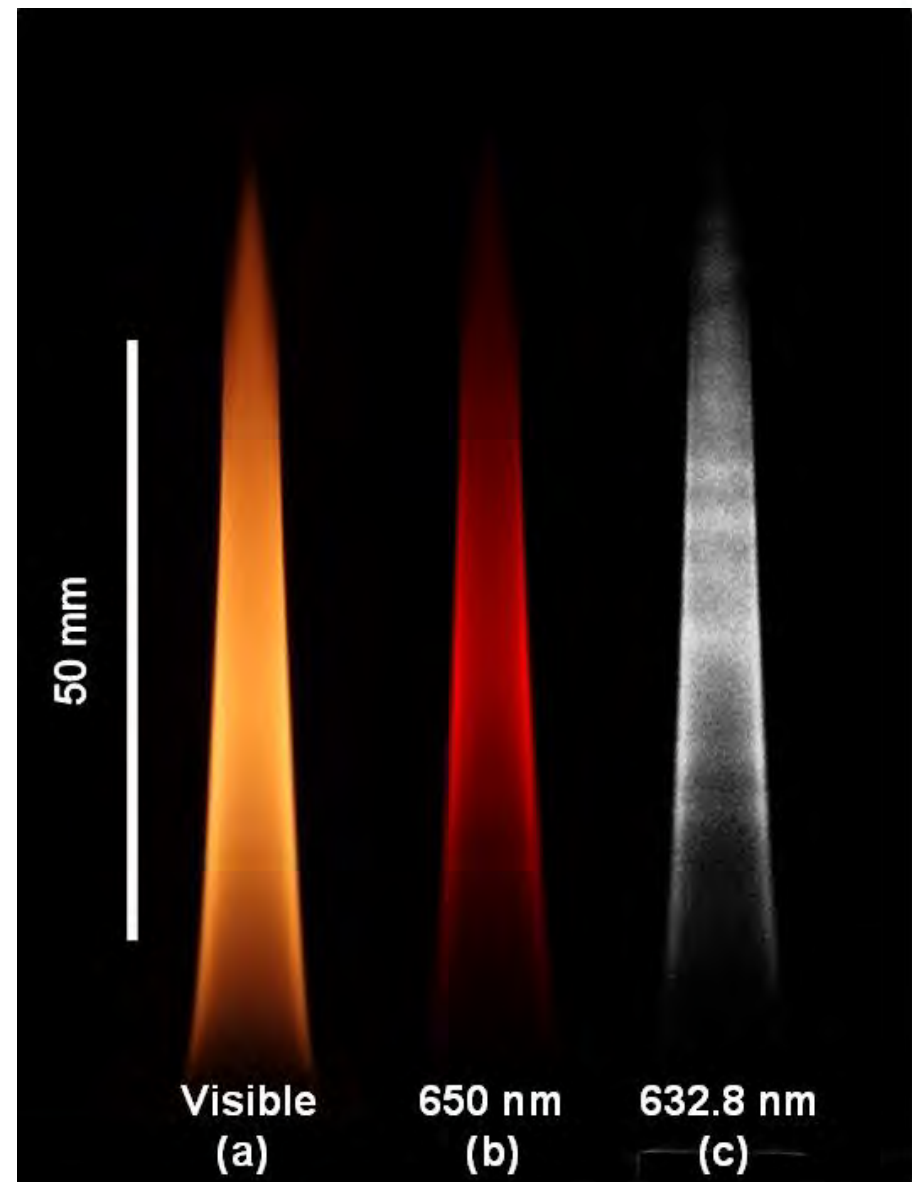
- Thermocouples are available as small as 25 μm .
- Soot particles have diameters of about 30 nm.
- Radiative losses in probes scale according to:

$$T_{gas} - T_{probe} = d Nu \sigma \varepsilon T_{probe}^4 / k$$

The thermal accommodation coefficient is a measure of non-continuum heat transfer effects. For soot it is nearly unity.

C₂H₄ flame

- Fuel: ethylene
- Oxidizer: coflowing air.
- Flame height: 88 mm
 - Steady
 - Optically thin
 - Axisymmetric



Abel transform

- Based on an exact solution
- Requires discretization

Line-of-sight integration of the flame property $f(r)$ is:

$$p(x) = \int_{-\infty}^{\infty} f(r) dy$$

Substituting y with x and r following $r^2 = x^2 + y^2$ yields:

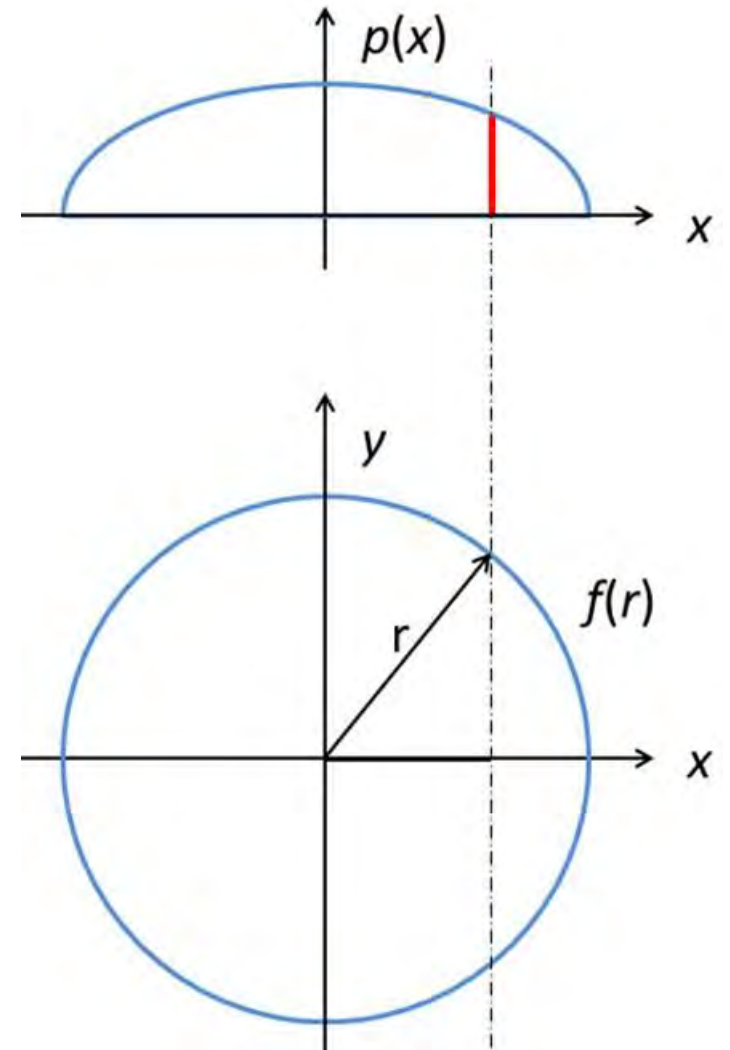
$$p(x) = 2 \int_x^{\infty} \frac{rf(r)}{\sqrt{r^2 - x^2}} dr$$

Analytical inverse of the above equation yields:

$$f(r) = -\frac{1}{\pi} \int_r^{\infty} \frac{p'(x)}{\sqrt{x^2 - r^2}} dx$$

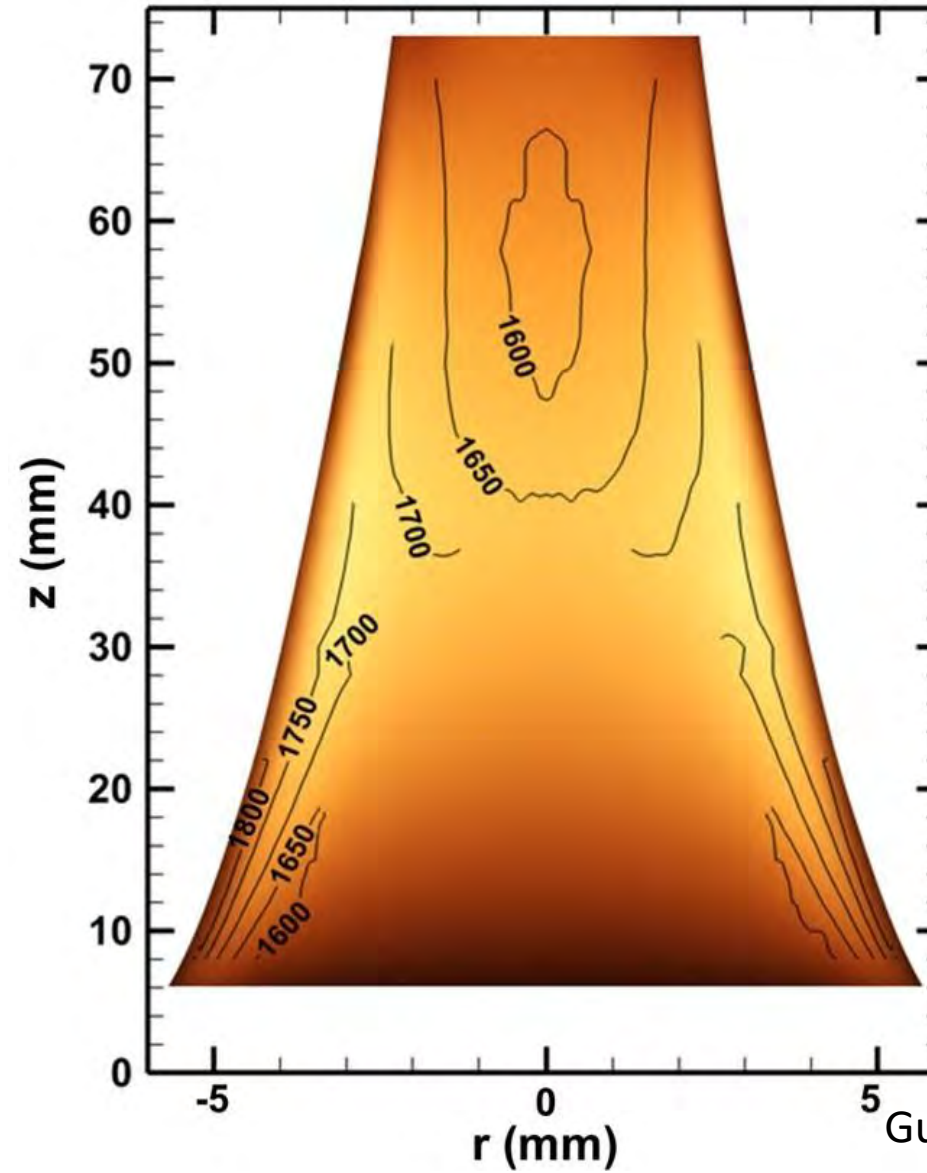
← Sensitive to noise

← Singularity at $x = r$

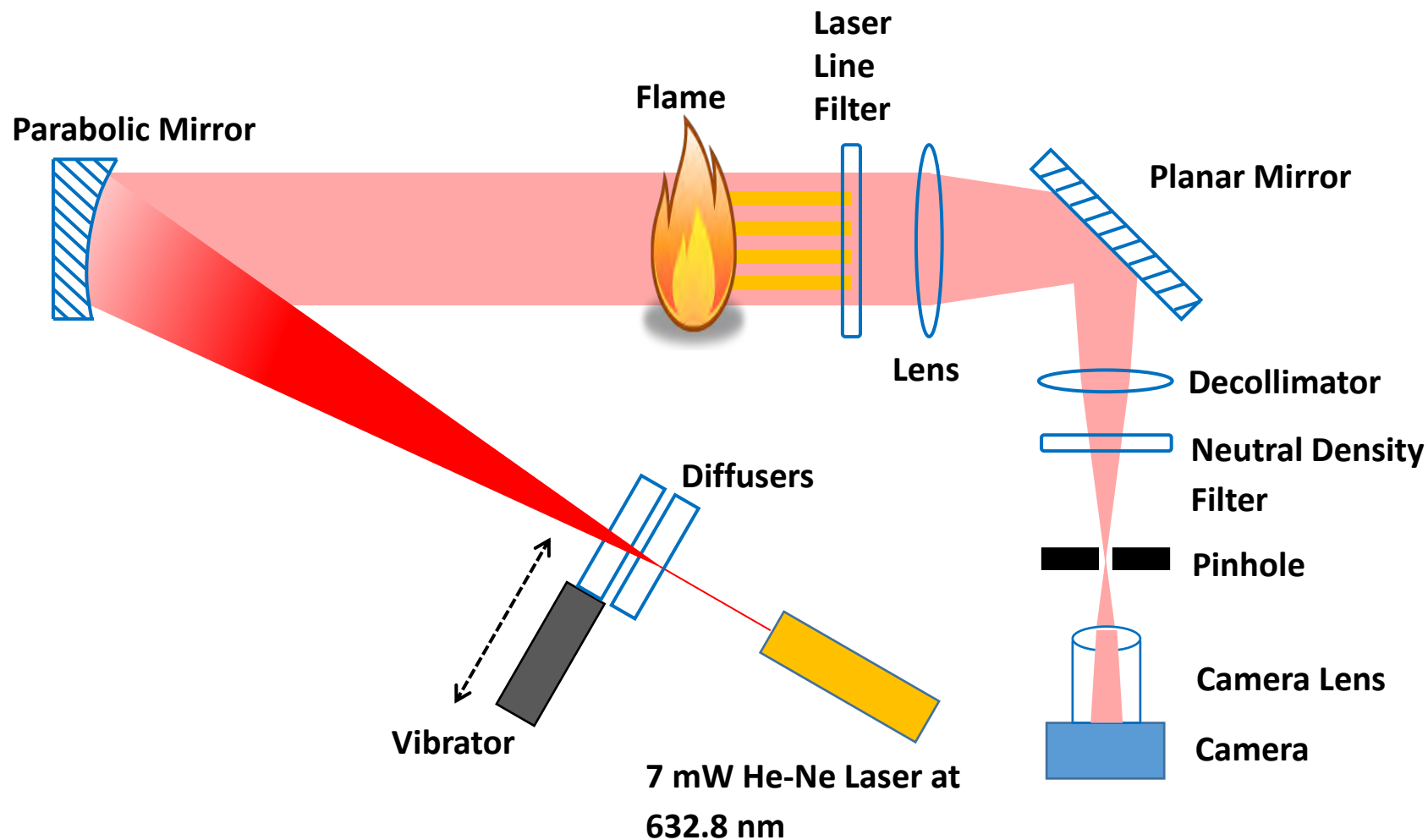


Soot pyrometry contours

- T range: 1600 – 1850 K.
- Spatial resolution: 23 μm
- Shutter time: 125 ms
- Uncertainty: ± 50 K
- Precision: ± 0.1 K

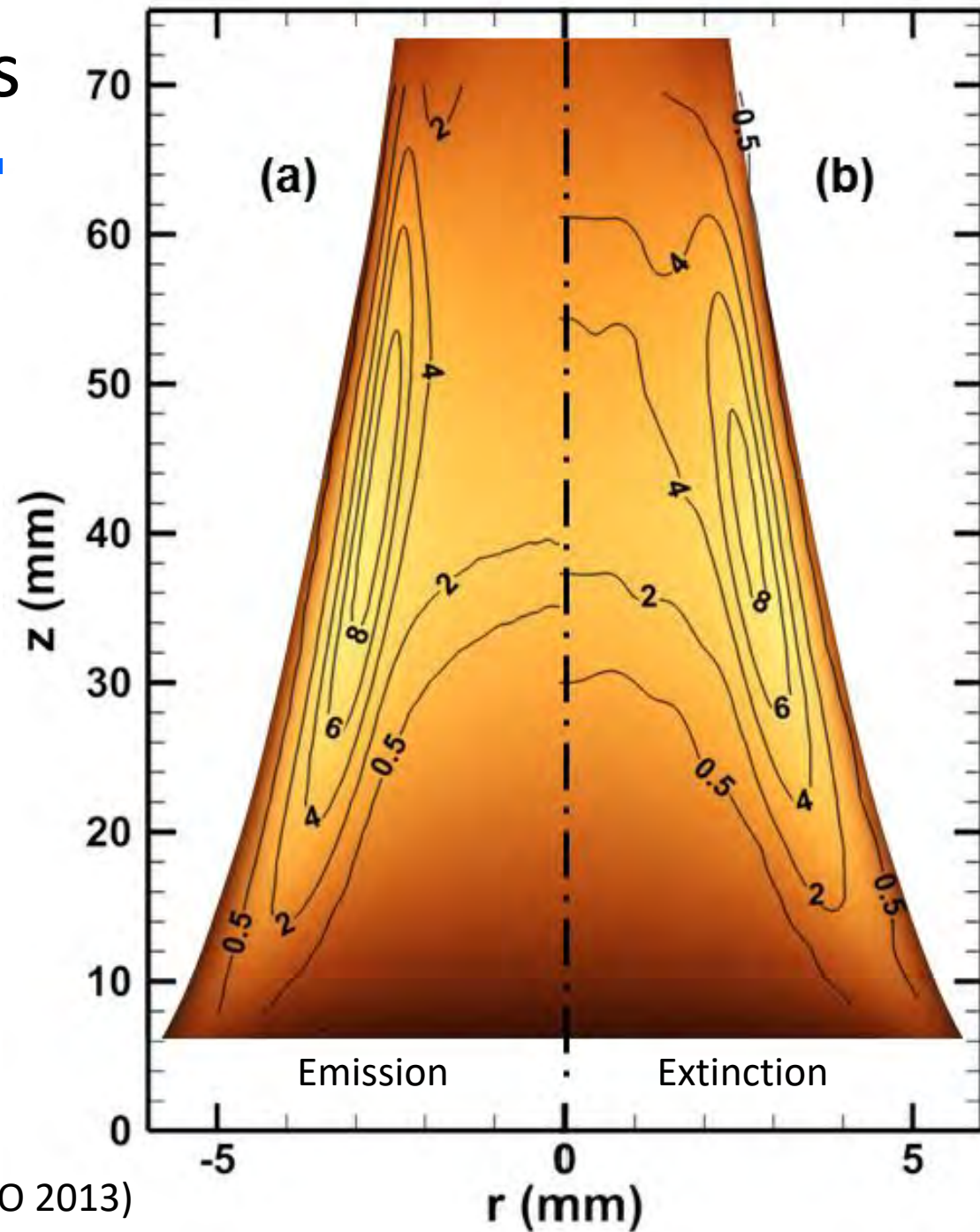


Laser extinction by soot



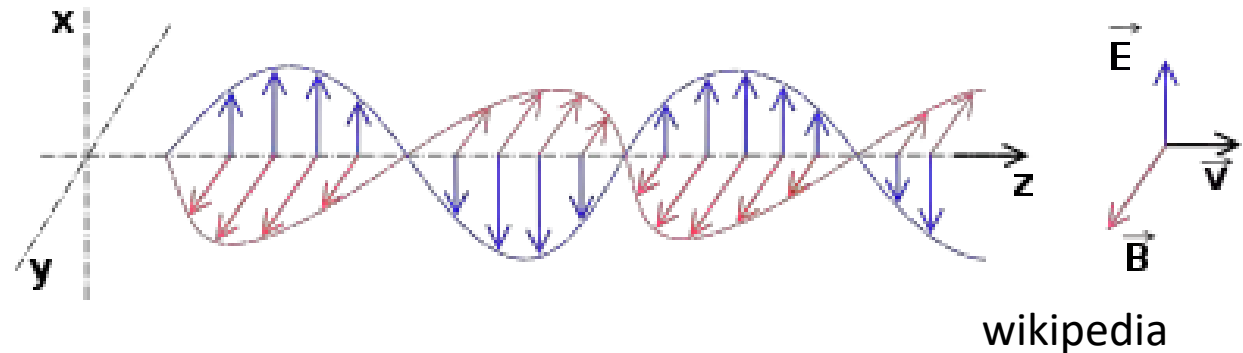
Soot volume fractions

	Emission	Extinction
f_s (ppm)	0.1-10	0.2-10
Res. (μm)	23	34
t (ms)	125	167
Precision (ppm)	$\pm 4 \times 10^{-4}$	$\pm 6 \times 10^{-4}$
Uncertainty	$\pm 30\%$	$\pm 10\%$

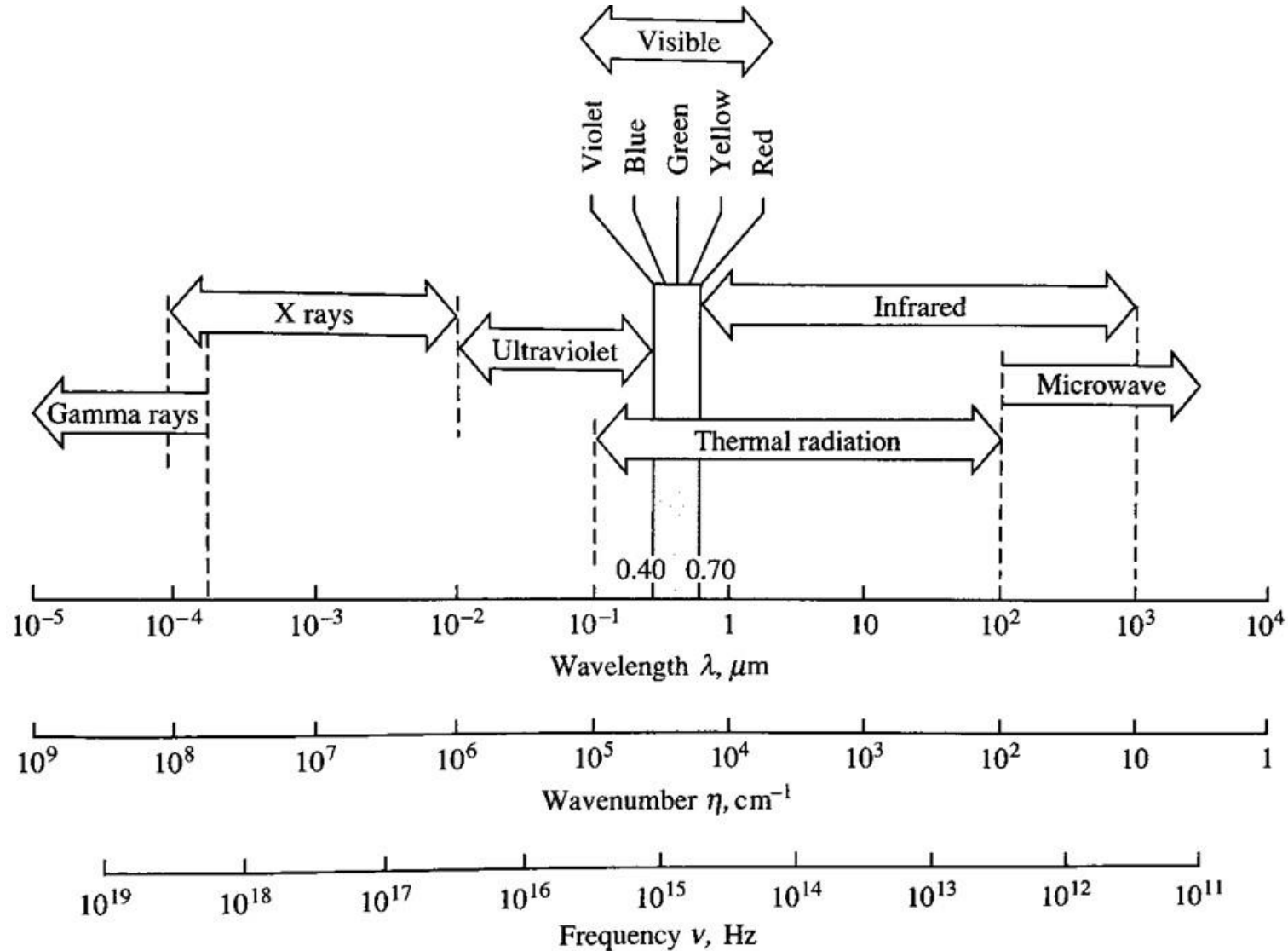


Thermal Radiation

- Radiation in fires is heat transfer via electromagnetic waves (EMR).
- All materials emit and absorb EMR.
- Unlike conduction and convection:
 - Radiation can span long distances
 - Radiation scales with T^4
 - Radiation requires no medium
 - Radiative properties of materials are very complex
- Radiation is a key factor in wildland fire spread (Rossi et al. FSJ 2011; Finney et al. PNAS 2015; Balbi et al. IJWF 2020).



EMR spectrum



$$\lambda = 1 / \eta$$

wavelength = 1 / wavenumber

Modest (1993)

Radiation from surfaces

Planck's Law gives the blackbody spectral emissive power:

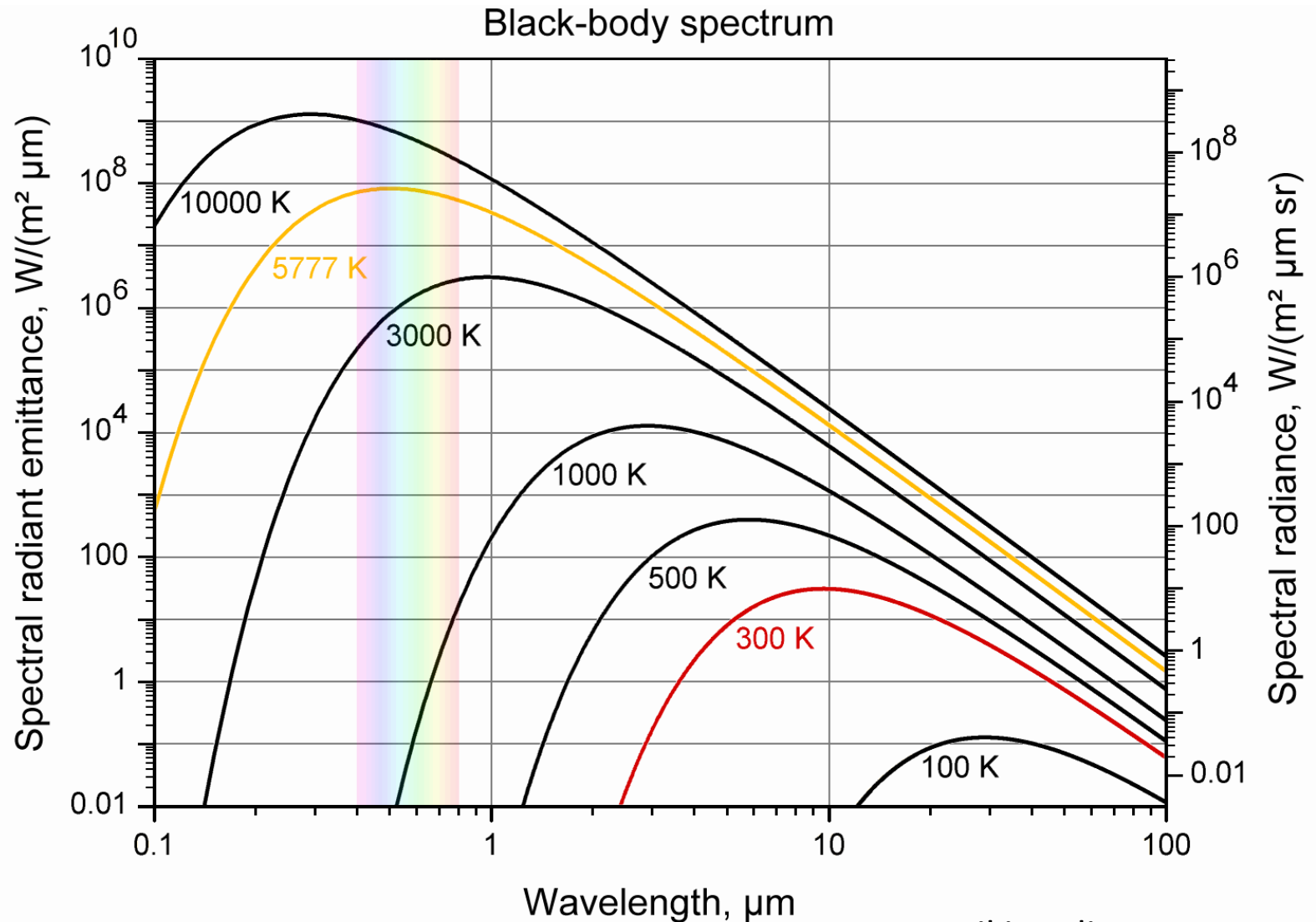
$$E_{b\lambda} = \frac{C_1}{\lambda^5 \left[\exp\left(\frac{C_2}{\lambda T}\right) - 1 \right]}$$

Integrating yields the total emissive power (the Stephan-Boltzmann Law):

$$E = \sigma T^4$$

Wein displacement law:

$$\lambda_{\max} = b / T$$



IR spot detectors

- Measure radiation (heat flux) from surfaces.
 - As temperature increases, radiation increases
- Range up to $\sim 3,300$ K,
- Must account for surface emissivity, reflection, ash, and smoke.



IR imagers

- There are two types of IR imagers:
- Thermal detectors: limited pixel counts (1.2 MP), cost up to \$20k.
- Quantum detectors: fast and sensitive, but most require cryogenic cooling, cost up to \$150k.
- IR lenses are costly, often made of calcium fluoride, sapphire, or germanium.
- IR imagers are common for satellite fire observations (Terra, Aqua, MODIS, EROS, GOES, VIIRS, etc.), with ~1 km resolution.
- From 5 μm – 8 μm there is atmospheric attenuation from H_2O and CO_2 .

Omega TIC, \$1,000

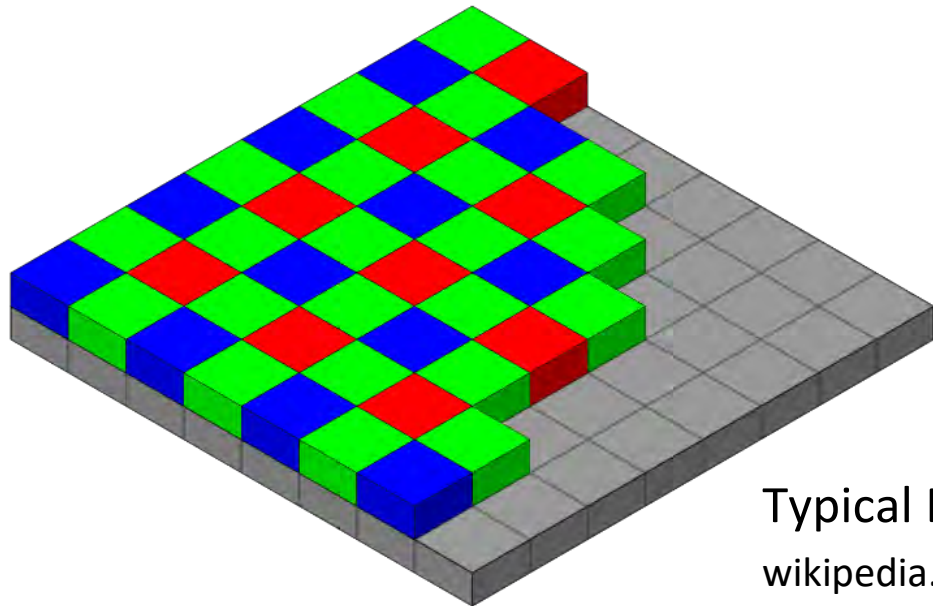


FLIR x6800sc
0.33 MP, \$100k



Color cameras

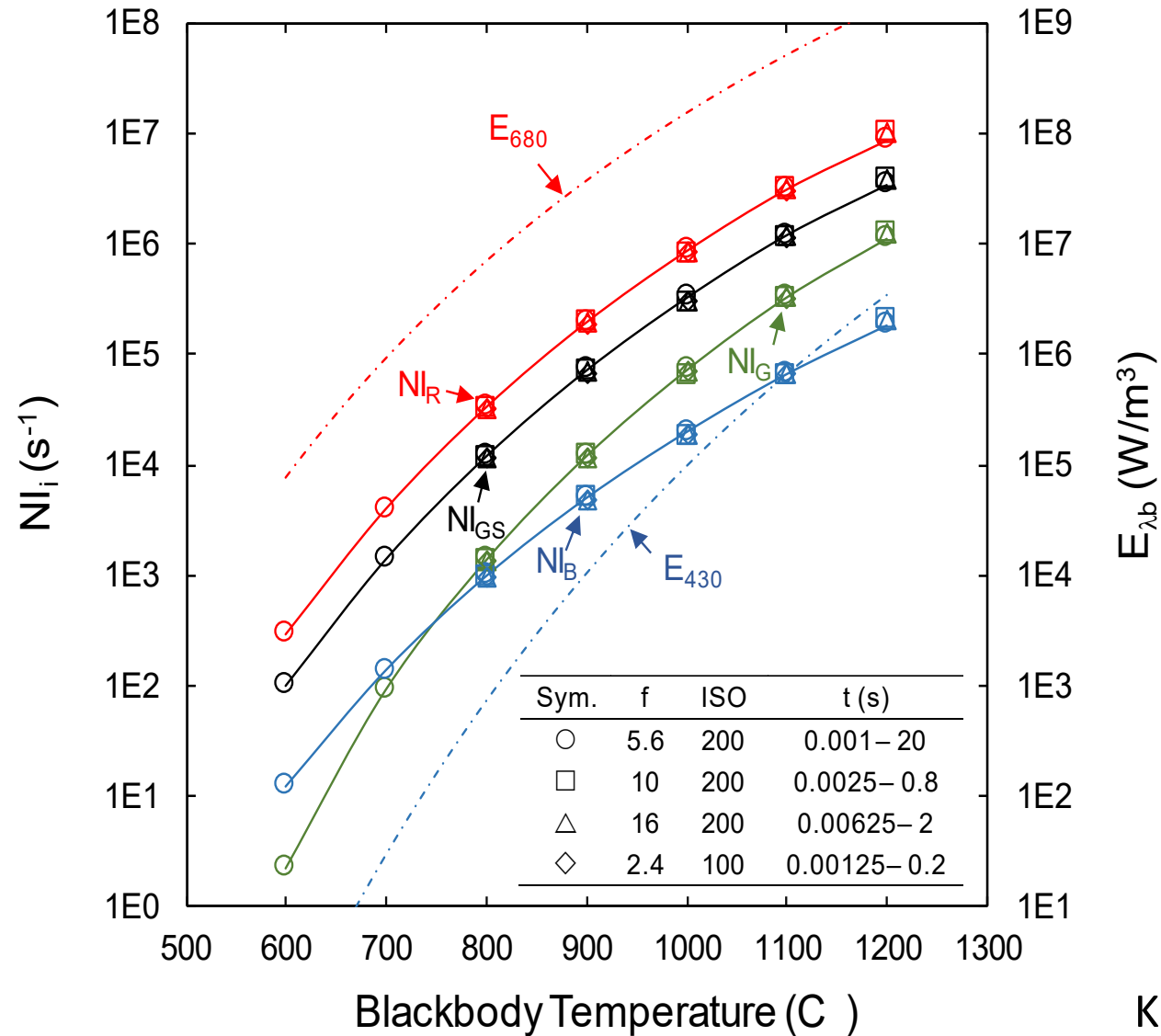
- Sony DSC-RX10 III, \$1,300
- 14 bit CMOS sensor, 20.1 MP
- Negligible dark current
- $FL = 24$ mm and $f = 2.4$



Typical Bayer filter array.
wikipedia.org

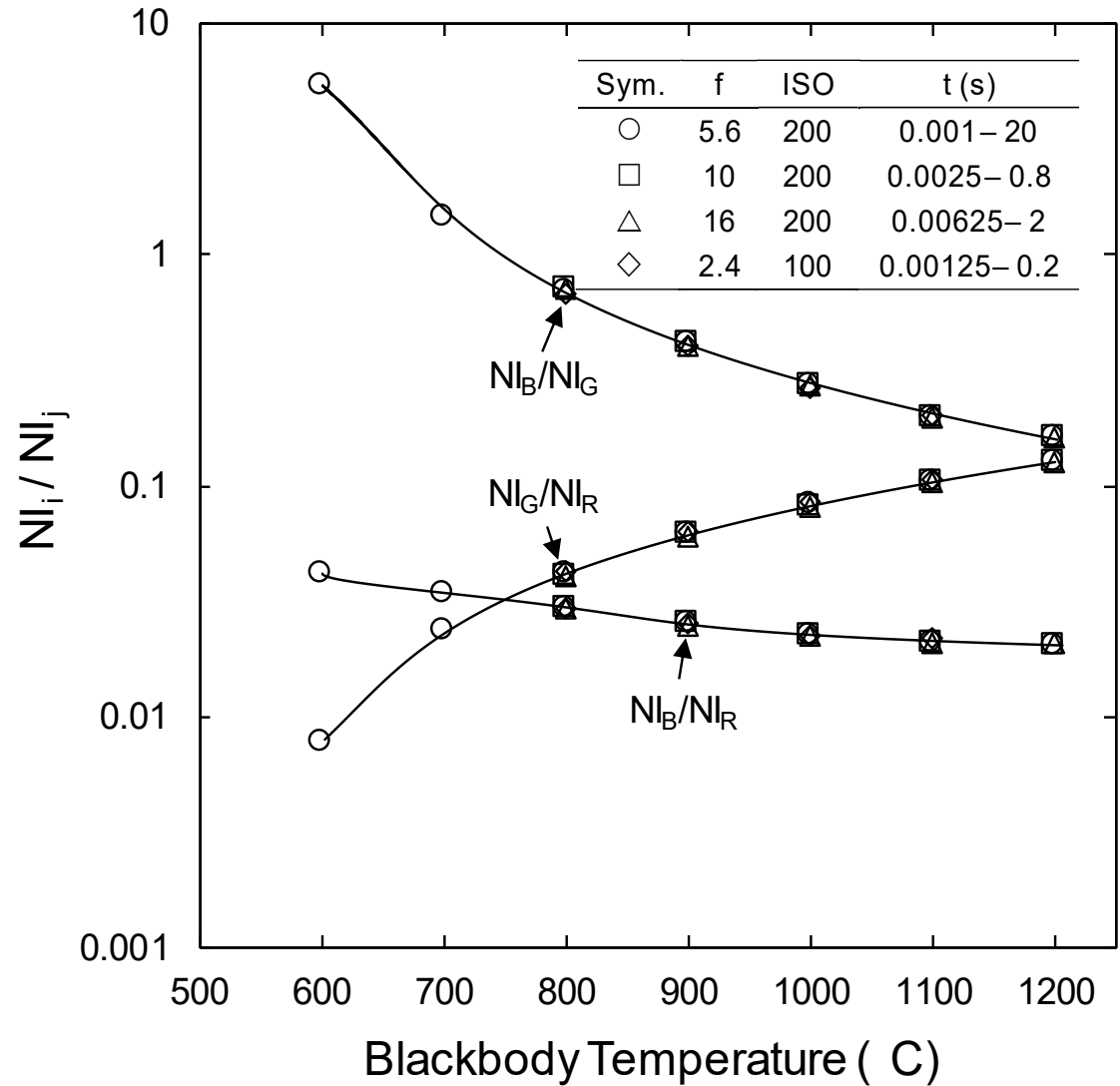


Single-band pyrometry



Kim and Sunderland (FSJ 2019)

Ratio pyrometry



Kim and Sunderland (FSJ 2019)



Single-band vs. ratio pyrometry for fires



	Single-Band Pyrometry	Ratio Pyrometry
Key Assumptions	<ul style="list-style-type: none">• $\epsilon \tau$ is a required input• Fire dwell time and image size must be known	<ul style="list-style-type: none">• $\epsilon \tau$ is the same at both wavelengths
Key Advantages	<ul style="list-style-type: none">• SNR is 18 times that of ratio pyrometry	<ul style="list-style-type: none">• No assumption of $\epsilon \tau$ is required• Neither fire dwell time nor image size must be known



Combine these to obtain the flame radiative flux at every pixel.

The spectral emissive power from an ember and passing through smoke is:

$$E_{\lambda} = \frac{C_1}{\lambda^5 \left[\exp \left(\frac{C_2}{\lambda T_{sb}} \right) - 1 \right]}$$

It can also be found from:

$$E_{\lambda} = \frac{C_1 \varepsilon \tau}{\lambda^5 \left[\exp \left(\frac{C_2}{\lambda T_{ratio}} \right) - 1 \right]}$$

Combining yields emissivity times transmittance:

$$\varepsilon \tau = \exp \left[-\frac{C_2}{\lambda} \left(\frac{1}{T_{sb}} - \frac{1}{T_{ratio}} \right) \right]$$

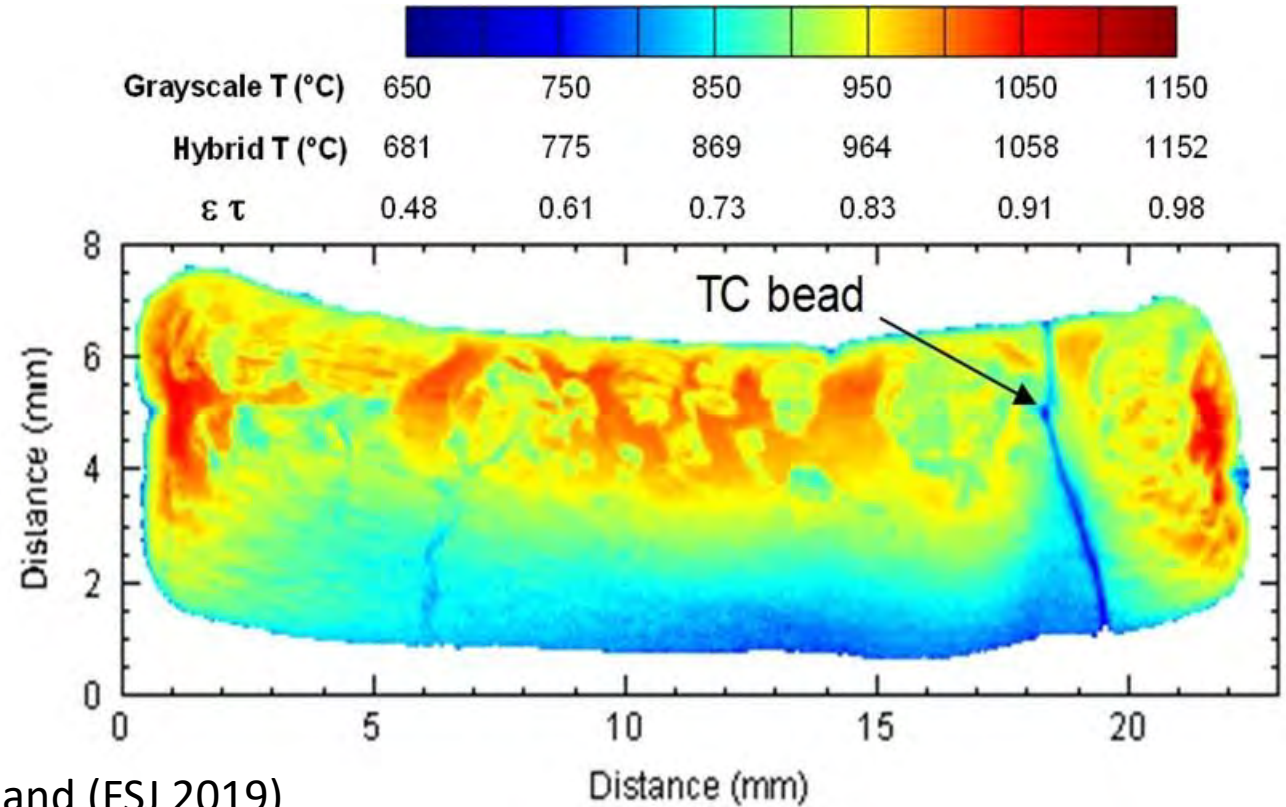
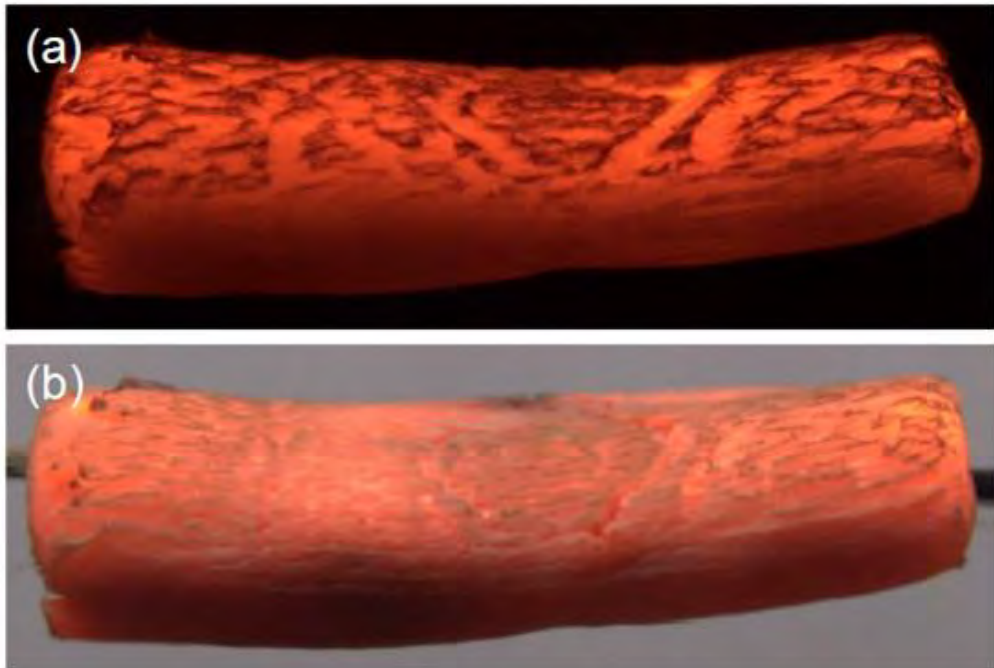
The heat flux is:

$$\dot{q}'' = \varepsilon \tau \sigma T_{ratio}^4$$



Medtherm

Ember pyrometry with color camera

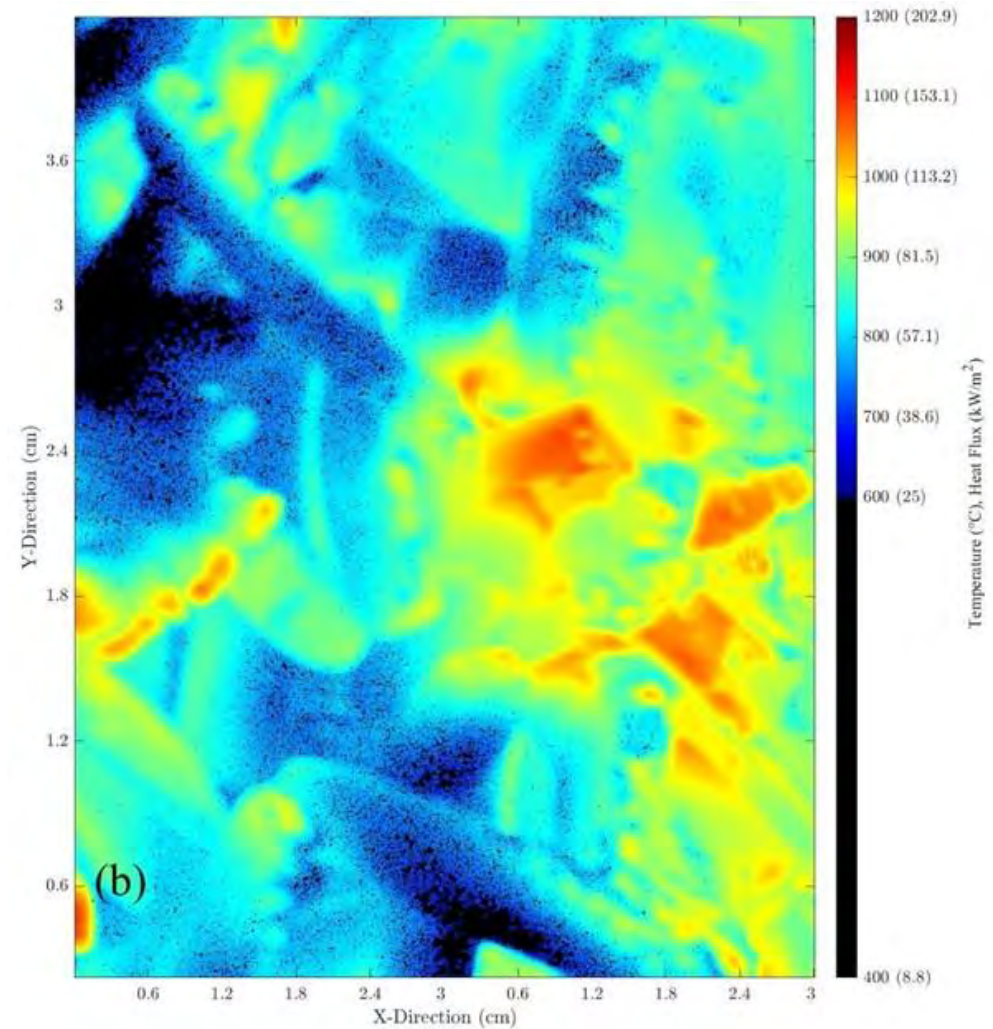


Kim and Sunderland (FSJ 2019)

Heat fluxes of ember piles



Color image of ember pile



Temperature and heat flux

Tlemsani et al. (2023)



Thin-filament pyrometry

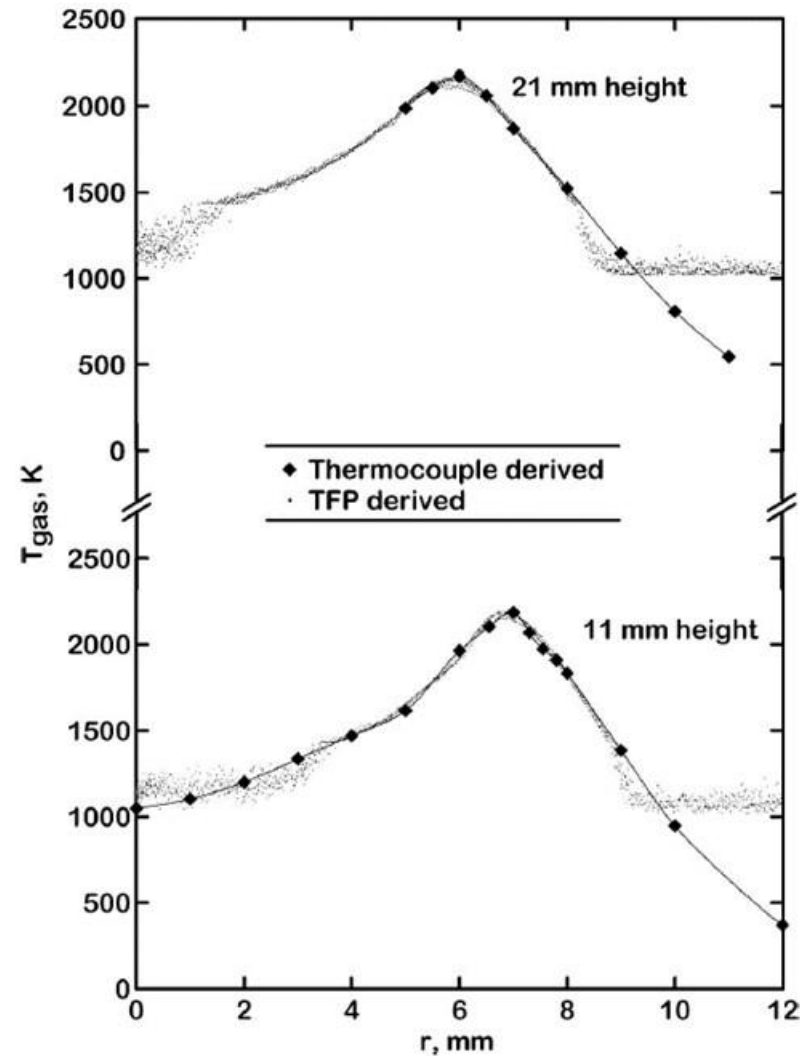
- SiC fibers, 15 μm diameter
- Filament emissivity: 0.88
- Radiation correction is required:

$$h (T_{gas} - T_{fiber}) = \sigma \varepsilon (T_{fiber}^4 - T_{\infty}^4)$$

$$Nu = h d_{fiber} / k_{gas}$$

$$Pe = u d_{fiber} / \alpha_{gas}$$

$$Nu = [0.8237 - 0.5 \ln (Pe)]^{-1}$$



Maun et al. (AO 2007)





Radiation in absorbing, emitting, and scattering media



Every point in space can interact with every other point – at the speed of light.
Every wavelength, species, and temperature can behave differently.

Many radiative transport equations (RTEs) are integro-differential equations, e.g.:

$$\begin{aligned} \mu \frac{dL_v}{d\delta_v} = & L_v(\delta_v, \mu, \phi) - (1 - \kappa_v) \int_0^{2\pi} d\phi' \int_{-1}^{+1} L_v(\delta_v, \mu', \phi') \{ p_v(\delta_v, \mu, \phi, \mu', \phi') / 4\pi \} d\mu' \\ & - (1 - \kappa_v) E_v^0 \exp\left(-\frac{\delta_v}{\mu_0}\right) \{ p_v(\delta_v, \theta, \phi, \theta^0, \phi^0) / 4\pi \} \\ & - \kappa_v B_v(\delta_v). \end{aligned}$$



Schwarzchild equation



In an absorbing gas or aerosol, radiative intensity decreases with distance as:

$$d I / d x = - \kappa I ,$$

where κ = absorption coefficient, aka attenuation coefficient or extinction coefficient.

This is the simplest RTE

Integrate, assuming constant κ , to obtain the Lambert-Beer-Bouger Law,

$$\frac{I}{I_0} = e^{-\kappa L} \equiv \tau ,$$

where τ is transmittance, aka transmissivity.

The path absorptivity is found from: $\alpha + \tau = 1$

Schwarzchild and Lambert-Beer-Bouger are often written in spectral form.



Optical depth

Optical depth, aka optical thickness, is

$$\tau \equiv \kappa L ,$$

and is dimensionless.

$$0 \leq \tau \leq \infty$$

$\tau \ll 1 \leftrightarrow$ optically thin

$\tau \gg 1 \leftrightarrow$ optically thick



Radiation from flames

The spectral radiative power from a flame is:

$$E_{\lambda} = \varepsilon_{\lambda} \frac{C_1}{\lambda^5 [\exp(\frac{C_2}{\lambda T}) - 1]}, \text{ where}$$
$$\varepsilon_{\lambda} = 1 - e^{-\kappa_{\lambda} L}$$

An integration over all λ yields

$$E = \sum \varepsilon_i \sigma T^4, \text{ with}$$

$$\varepsilon_i = 1 - e^{-\kappa_p p L},$$

where the summation is over all the species, κ_p is the Planck mean absorption coefficient, p is partial pressure.

There are three type of flame absorption/radiation models:

1. Line-by-line spectral models, e.g., statistical narrow band (SNB).
2. Band spectral models, e.g., wide-band models (WB).
3. Global models, e.g., weighted sum of gray gas (WSGG).

A reasonable approximation is the global radiant fraction model (Ahmed 2023), where $\chi_r = 15\%$ (alcohols) to 50% (aromatics).



Aerosol scattering

An aerosol is a mixture of gas and small liquid or solid particles.

Aerosols can interact with light in unusual ways.

Particle regime	Particle diameter	Scattering model	Model complexity
Small	$< 0.1 \lambda$	Rayleigh	Simple
Medium		Mie	Complex
Large	$> \lambda$	Geometric optics (ray tracing)	Simple



Soot extinction

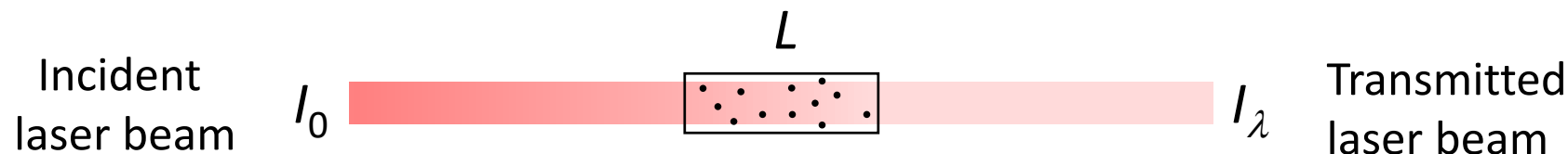
- Rayleigh scattering for soot yields

$$\kappa_{\lambda} = 6 \pi E(m) f_s / \lambda ,$$

with refractive index absorption function $E(m) = 0.26$
for soot with a refractive index of $m = 1.57 - 0.56 i$

Note that soot emissivity also scales with $1 / \lambda$.

- From Lambert-Beer-Bouguer Law: $\frac{I_{\lambda}}{I_0} = e^{-\kappa_{\lambda} L}$



ASTM E662 smoke chamber

Also NFPA 258, IEC 60695-6-30

ASTM E662 features:

A sealed chamber

Only one surface exposed

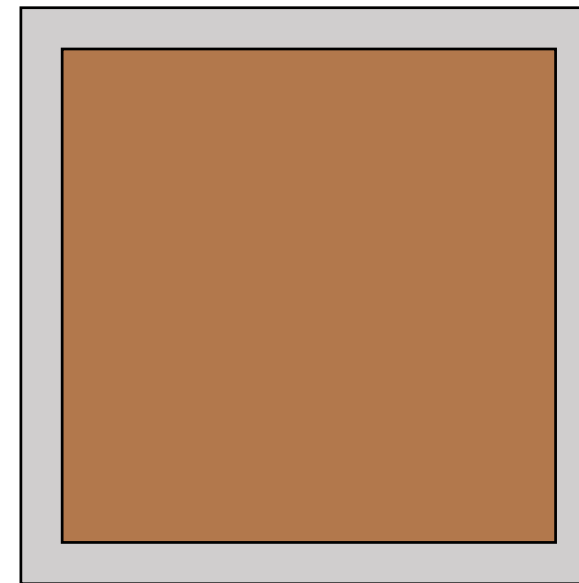
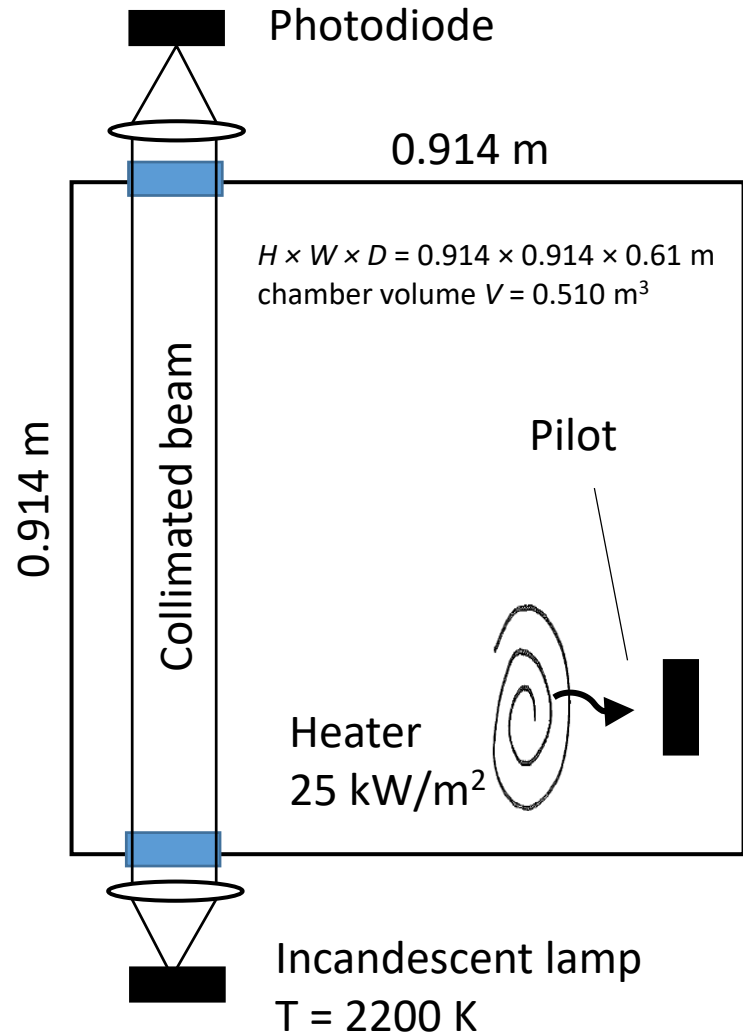
A vertical light beam

Quantitative measures, namely

D_m , D_{mass} , and SOI .



Smoke chamber



Specimen size: 76.2 × 76.2 mm
 Open area: 65.1 × 65.1 mm
 Al foil on back, sides, and top edge
 Thickness ≤ 25 mm

Summary

- Soot is formed only in flaming combustion, but other solid aerosols are often called soot.
- The complexity of soot is infinite, but the best simple models have changed little since 2000.
- The small size of soot makes it ideal for pyrometry.
- Radiative emissions from fires vary from 15 – 50%.
- Radiation can dominate wildland fire spread rates.
- Accurate measurements and simulations of fire radiative behavior are challenging.



Craighill bonfire

<https://twitter.com/EmmaVardyTV/status/1414393963075837956>